

Fig. 2 Nongray error for selective emitter-type material.

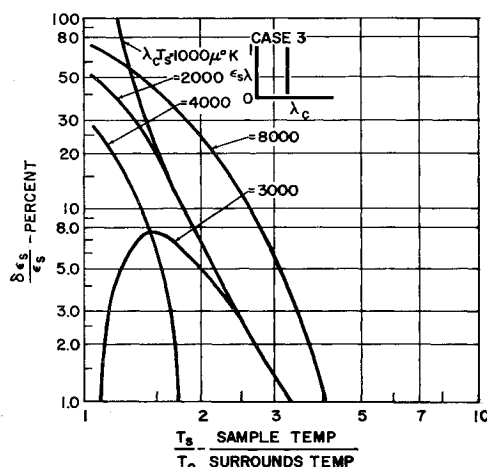


Fig. 3 Nongray error for spike emitter-type material.

"spike" or single emittance line. Edwards and Nelson¹ presented partial results for case 1.

Making the substitutions

$$F(Z) = C_1 Z^{-5} \{ [\exp(C_2/Z)] - 1 \} = T^{-5} E(\lambda, T) \quad (10a)$$

$$Z = \lambda T \quad (10b)$$

$$T^* = T_s / T_0 \quad (10c)$$

in Eq. (8) and applying the limits from Eq. (9), the nongray error for the cases considered becomes

Case 1

$$\frac{\delta \epsilon_s}{\epsilon_s} \geq \frac{1}{[(T^*)^4 - 1]} \left[\int_{\lambda_c T_0}^{\lambda_c T_0 T^*} F(Z) dZ / \int_0^{\lambda_c T_0 T^*} F(Z) dZ \right] \quad (11a)$$

Case 2

$$\frac{\delta \epsilon_s}{\epsilon_s} \geq \frac{1}{[(T^*)^4 - 1]} \left[\int_{\lambda_c T_0}^{\lambda_c T_0 T^*} F(Z) dZ / \int_{\lambda_c T_0 T^*}^{\infty} F(Z) dZ \right] \quad (11b)$$

Case 3

$$\frac{\delta \epsilon_s}{\epsilon_s} \geq \frac{1}{[(T^*)^4 - 1]} \frac{F(\lambda_c T_0) - T^* F(\lambda_c T_0, T^*)}{T^* F(\lambda_c T_0, T^*)} \quad (11c)$$

The results of numerical computation of Eq. (11) are shown in Figs. 1-3 for a range of T_s^* and $\lambda_c T_s$. If $\lambda_c T_s$ is equal to 3000, the material has an emittance of 0.27 if it is a case 1 material and 0.73 if it is a case 2 material; if the value of $\lambda_c T_s$ is 6000, the corresponding emittances are 0.73 and 0.27, respectively. The extremes of $\lambda_c T_s$ cannot be ignored, how-

ever. For both case 1 and 2 materials, the extremes of $\lambda_c T_s$ are highly reflective materials, and these extremes indicate the possible effect of a surface film that is transparent through almost all of the wavelengths involved in the emission. The nongray error can be minimized by maintaining a large value of T_s^* in the instance of case 1 or 3. The error for case 2 is significant for values of T_s^* as large as 5-10.

Reference

- Edwards, D. K. and Nelson, K. E., "Maximum error in total emissivity measurements due to nongrayness of samples," ARS J. 31, 1021-1022 (1961).

Erratum: "Electrical Discharge Across a Supersonic Jet of Plasma in Transverse Magnetic Field"

STERGE T. DEMETRIADES* AND PETER D. LENN†
Northrop Corporation, Hawthorne, Calif.

[AIAA J. 1, 234 (1963)]

LINE 7 of the above paper should read "... at a velocity of approximately 3×10^3 ," rather than " 3×10^4 ." The value was correct in galley proof, but the error occurred in making another correction in this paragraph in page proof.

* Head, Plasma Laboratories. Associate Fellow Member AIAA.

† Member of Research Staff, Plasma Laboratories. Member AIAA.

Moment of Momentum by Direction Cosines

JOSEPH STILES BEGGS*
University of California, Los Angeles, Calif.

THE equation relating the sum of the moments acting on a rigid body to the time rate of change of its moment of momentum can be written

$$\mathbf{M} = [C_{01}][\dot{C}_{10}][I]_1[\dot{C}_{01}][\dot{C}_{10}] + [I]_1([\dot{C}_{01}][\dot{C}_{10}] + [C_{01}][\dot{C}_{10}]) + m \mathbf{r}_1 \times \mathbf{a} \quad (1)$$

where $X_0 Y_0 Z_0$ is an inertial Cartesian coordinate system and $X_1 Y_1 Z_1$ is any coordinate system fixed in the body. Its origin is O_1 .

$[C_{01}]$ is the direction cosine matrix taken from the transformation matrix that transforms the coordinates of a point from system 0 to system 1. $[C_{10}] = [C_{01}]'$, the transpose of $[C_{01}]$. $[I]_1$ is the inertia tensor of the body computed in system 1. \mathbf{r}_1 is the position vector of the center of mass of the body measured from O_1 , and \mathbf{a} is the acceleration of O_1 relative to $X_0 Y_0 Z_0$.

\mathbf{M} is the sum of the moments, about O_1 , of all the external forces acting on the body. Equation (1) gives its components in system 1.

The curved brackets denote the operation of forming (either manually or by computer program), a column matrix

Received May 9, 1963.

* Professor of Engineering.